

## LOGISTIC MODEL

- by Pierre Verhulst (1838)- The rate of population increase may be limited, i.e., it may depend on population density:

- Logistic equation  $r = r_0(1 - \frac{N}{K})$

- At low densities ( $N \ll K$ ), the population growth rate is maximum =  $r_0$ .

$$\frac{dN}{dt} = rN = r_0N(1 - \frac{N}{K})$$

- Population growth rate declines with population numbers,  $N$ , and reaches 0 when  $N = K$ .

Parameter  $K$  is the upper limit of population growth (carrying capacity).



- **Carrying capacity  $K$**  - The maximum number of individuals that can live in a population stably; numbers larger than this will suffer a negative population growth until eventually reaching the carrying capacity, whereas populations smaller than the carrying capacity will grow until they reach it.

- **Three possible model outcomes**

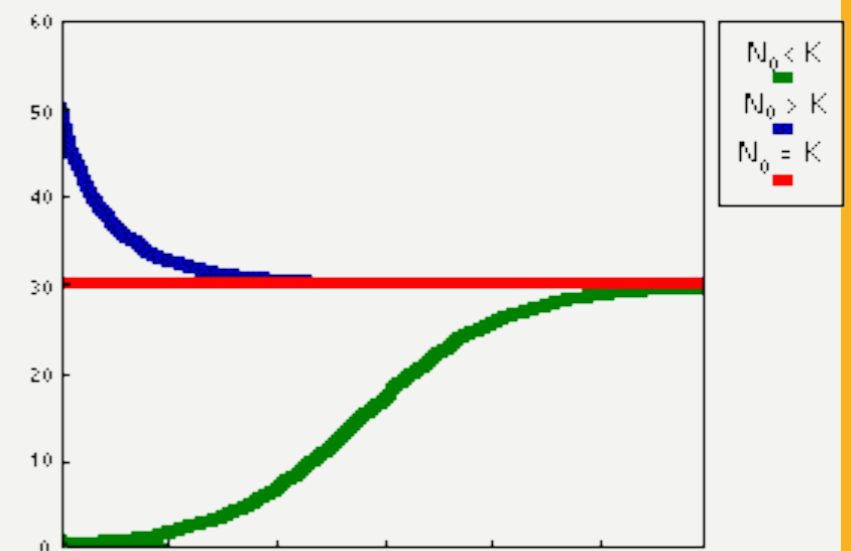
Population increases and reaches a plateau ( $N_0 < K$ ). This is the logistic curve.

Population decreases and reaches a plateau ( $N_0 > K$ )

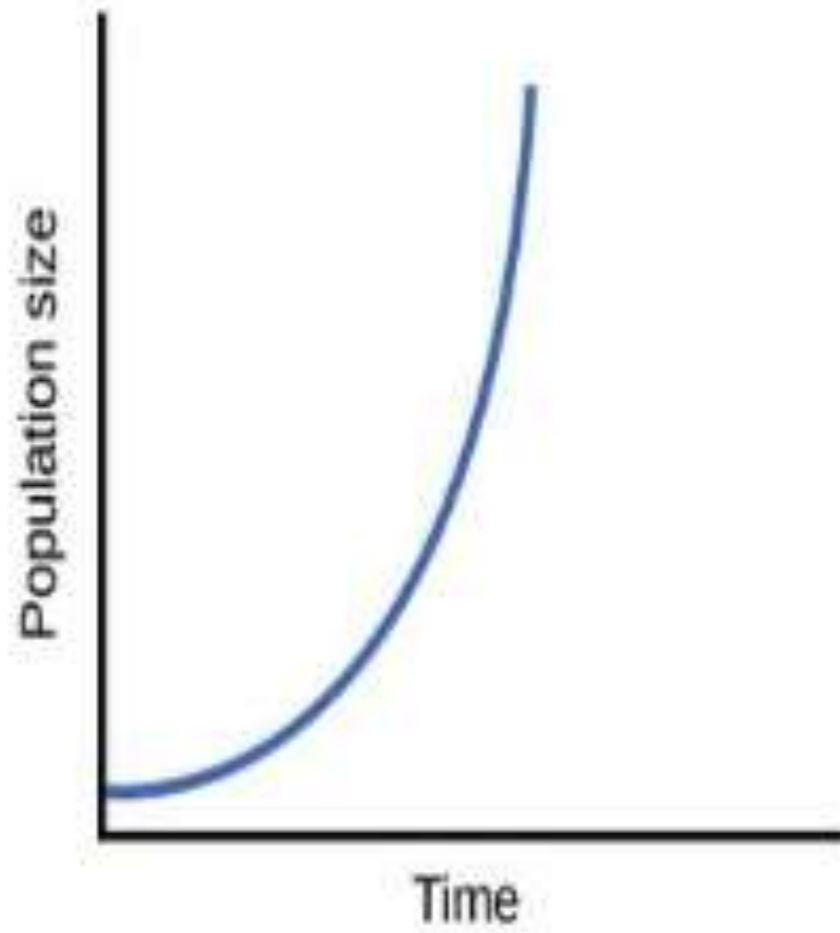
Population does not change ( $N_0 = K$  or  $N_0 = 0$ )

- **Assumptions of the logistic model:**

- Each individual has identical ecological properties
- Instantaneous response to environmental change
- Limited space and constant food supply
- Age distribution is stable



### Exponential Growth



### Logistic Growth

